Name: <u>Solution Key</u> Student ID: ____

- 1. (4 points) Suppose that |A| = m and |B| = n, give the following cardinalities:
 - (a) $|\mathcal{P}(\mathcal{P}(\mathcal{P}(A)))|$ (b) $|\mathcal{P}(A \times B)|$ (c) $2^{2^{2^m}}$ (c) 2^{m*n}
- 2. (6 points) If $A = \{1, 2\}, B = \{z\}$, give the power sets of A, B, and $A \times B$

$$\begin{split} P\left(A\right) &= \left\{ \emptyset, \left\{1\right\}, \left\{2\right\}, \left\{1,2\right\} \right\} \\ P\left(B\right) &= \left\{\emptyset, \left\{z\right\}\right\} \\ P\left(A \times B\right) &= \left\{\emptyset, \left\{(1,z)\right\}, \left\{(2,z)\right\}, \left\{(1,z), (2,z)\right\}\right\} \end{split}$$